Vocabulary

Zero Exponents	Negative Exponents	Product of Powers	Pov
Power of a Product	Power of a Quotient	Exponential Expression	

Power of a Power

Laws of Exponents

- Zero power and Negative Exponents: $a^0 = 1, a \neq 0$ $a^{-n} = \frac{1}{a^n}$ and $\frac{1}{a^{-n}} = a^n, a \neq 0$
- **Product of Powers Property:** $a^m \bullet a^n = a^{m+n}$
- **Power of a Power Property:** $(a^m)^n = a^{m \cdot n}$
- **Power of a Product Property:** $(a \bullet b)^m = a^m \bullet b^m$
- Quotient of Powers Property: $\frac{a^m}{a^n} = a^{m-n}, a \neq 0$

• Power of Quotient Property:
$$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m}, b \neq 0$$

What should you be able to do?

- Simplify exponential expressions (both numerical and algebraic) using laws of exponents and properties of exponents
- Simplify expressions that have fractional exponents
- Solve for a variable using the inverse of its exponent
- Solve for variable exponents

Practice Problem Set

Simplify each exponential expression. All simplified expressions must be written with positive exponents.

1.
$$3^2 \bullet 3$$
 2. $(2^{-2})^2$ 3. $(\frac{3}{2})^{-3}$ 4. $(\frac{4^0 \bullet 5^3}{5^4})^{-2}$

5.
$$\frac{x^4 \bullet x^{-6}}{x^5}$$
 6. $\left(\frac{1}{2}x^2\right)^3$ 7. $-(x^3y)^2$ 8. $7x^{-5}y^{-1}$

9.
$$\left(\frac{2x}{x^2}\right)^4$$
 10. $\frac{1}{11x^{-2}y^{-7}}$ 11. $(2^{-1}x^{-10})^4$ 12. $(-2x^2y)(x^3y)^{-4}$
13. $\frac{x^{-4}}{(12y^2)^{-2}}$ 14. $\left(\frac{x^{-2}y}{x^8y^{-5}}\right)^3$ 15. $\frac{3xy^4}{2x^5y} \cdot \frac{6x^{-3}y^2}{4y}$ 16. $\left(\frac{4x^2y^{-1}}{xy}\right)^{-3} \div \frac{x^6y^2}{y^4}$
17. $64^{\frac{3}{2}}$ 18. $27^{\frac{-4}{3}}$ 19. $(\frac{125}{-64})^{\frac{2}{-3}}$ 20. $(\frac{625x^8y^{12}}{81w^4})^{\frac{-3}{4}}$

Solve for the unknown exponent.

21.
$$8^{x+6} = 8^{11}$$
 22. $(\frac{1}{27})^{16} = 3^{2x+4}$ 23. $64^{x+5} = 32^{2x+1}$

24.
$$(\frac{1}{4})^{2x} = (16)^{5x-12}$$
 25. $\frac{1}{m^3} = (m^b)^{\frac{6}{5}}$ 26. $25^{c-4} = (\frac{1}{125})^{4c+5}$