1.

Essential Question: What are the properties of real numbers and how can we use them to demonstrate equivalence?

## Do Now: Let's see what you learned from the flip. Complete #'s 1 - 6. $\subseteq$

x + 9 = 9 + x is an example of which property?



- (1) identity property of addition
- (3) commutative property of addition
- (2) associative property of addition
- (4) distributive property
- Which is an example of the associative property of multiplication? 2.

$$(1)$$
 6 + 7 = 7 + 6

$$(3) \times \bullet (8 \bullet 3) = (\times \bullet 8) \bullet 3$$

(2) 
$$6(7 + 3) = 6(7) + 6(3)$$

(4) (ab) 
$$\bullet$$
 c = c  $\bullet$  (ab)

- 3. What property is illustrated by the statement -y + y = 0?
  - (1) identity property of addition
- (2) associative property of addition
- (3) commutative property of addition
- (4) inverse property of addition
- 4. Which number represents the additive inverse of  $-3\frac{3}{4}$ ?

(1) 
$$\frac{4}{15}$$

(2) 
$$-\frac{4}{15}$$

(3) 
$$3\frac{3}{4}$$

- 5. Which property is illustrated by the statement?  $2x \cdot \frac{1}{2x} = 1$ 
  - (1) identity property of multiplication

  - (3) commutative property of multiplication
- (2) associative property of multiplication
- (4) inverse property of multiplication
- Which of the following equations illustrates an identity property?

$$(1) 5(2 + 3) = 10 + 15$$

$$(2) 11 + 0 = 11$$

(4) 
$$\frac{1}{6} \bullet 6 = 1$$

## Applications with Properties

7. Sarah used the steps shown below to solve the following equation.

$$\frac{3}{4} \bullet 7a \bullet \frac{4}{3} = 49$$

Step 1: 
$$\frac{3}{4} \bullet \frac{4}{3} \bullet 7a = 49$$

**Step 2:** 
$$1 \bullet 7a = 49$$

**Step 3:** 
$$7a = 49$$

**Step 4:** 
$$a = 7$$

- a. Which step demonstrates the commutative property of multiplication?
- b. Which property does Sarah use to go from Step 2 to Step 3?

8. The following portion of a flow diagram shows that the expression  $\mathbf{ab} + \mathbf{cd}$  is equivalent to the expression  $\mathbf{dc} + \mathbf{ba}$ .

$$ab + cd \longrightarrow ba + cd \longrightarrow ba + dc \longrightarrow dc + bc$$

Fill in each circle with the appropriate symbol:

C+ (for the "Commutative Property of Addition")

C× (for the "Commutative Property of Multiplication")

A. 
$$x(z+y)$$
 B.  $xz+xy$  C.  $zx+yx$  D.  $yx+zx$ 

$$B. xz + xy$$

$$C. zx + yx$$

D. 
$$yx + zx$$

## Which statement is false?

- (1) Expression B is equivalent to expression C.
- (2) Expression C is equivalent to expression D but not to expression A.
- (3) Expressions B, C and D are equivalent.
- (4) All the expressions are equivalent.
- 10. The following is a proof of the algebraic equivalence of  $c(a+b) \cdot \frac{1}{ca}$  and  $\frac{cb}{ca} + 1$ .
  - a. Fill in the missing lines with the full name of the property being used.

$$c(a+b) \cdot \frac{1}{ca}$$

$$= (ca+cb) \cdot \frac{1}{ca}$$

$$= (cb+ca) \cdot \frac{1}{ca}$$

$$= \frac{cb}{ca} + \frac{ca}{ca}$$

$$= \frac{cb}{ca} + 1$$
Any number or term divided by itself is always 1

b. What is another way to prove that  $c(a+b) \cdot \frac{1}{ca}$  and  $\frac{cb}{ca} + 1$  are equivalent?

1. The following flow diagram shows that the expression (MV)Q is equivalent to the expression (VQ)M.

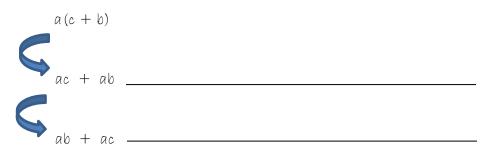


Fill in each circle with the appropriate symbol.

 $C_{x}$  = commutative property of multiplication

 $A_x$  = associative property of multiplication

2. Martha's proof to show the algebraic equivalence between a(c + b) and ab + ac is shown below. Examine the proof and indicate which properties Martha used in her process.



3. Franny measured the dimensions of the rectangular solid below and used the formula SA = 2lw + 2lh + 2wh to calculate its surface area. John did the same but he used the formula SA = 2(lw + lh + wh) to calculate the surface area. Do you think Franny and John will get the same answer? Explain why or why not.

