

Essential Question: How do we add and subtract polynomials?

Do Now: What did you learn from the Flip? Complete the table below.

Polynomial	Most Specific Name	Standard Form	Degree	Leading Coefficient	Constant Term
6	monomial	6	0	6	6
-2x	monomial	-2x	1	-2	0
9 + 3x	binomial	3x + 9	1	3	9
2x - 5 - x <sup>2</sup>	trinomial	-x <sup>2</sup> + 2x - 5	2	-1	-5
4x <sup>3</sup> - 8x	binomial	4x <sup>3</sup> - 8x	3	4	0
1 - 7x <sup>2</sup> + 6x + 2x <sup>3</sup>	polynomial	2x <sup>3</sup> - 7x <sup>2</sup> + 6x + 1	3	2	1

How do we determine the degree of a monomial with more than one variable?

Sum the exponents of the variables.

a)  $5x^2y^3$

Degree: 5

b)  $-3xy^3$

Degree: 4

c)  $7ab^3c^5$

Degree: 9

STOP HERE

### Adding Polynomials



How do we add polynomials? Consider:  $(8x^2 + 3) + (2x^2 - 6x + 4) + (-5x^2 - 7x)$

combine like terms

$$\begin{array}{r} \underline{8x^2} + 3 + \underline{2x^2} - 6x + 4 - \underline{5x^2} - 7x \\ \uparrow \qquad \qquad \qquad \uparrow \qquad \qquad \qquad \uparrow \\ 5x^2 - 13x + 7 \end{array}$$

Find the sum of the given polynomials. Represent your final answer in standard form.

1)  $(6 - 3t - t^4) + (9t + t^4) + 5t^2$

$$\begin{array}{r} \underline{6} - 3t - \underline{t^4} + 9t + \underline{t^4} + \underline{5t^2} \\ \uparrow \qquad \qquad \qquad \uparrow \qquad \qquad \qquad \uparrow \\ 5t^2 + 6t + 6 \end{array}$$

## Subtracting Polynomials



How do we subtract polynomials? Consider:  $(3x^3 - x^2 + 8) - (2x^2 + 3x + 1)$

- distribute the negative to all terms in the ( )
- combine like terms

$$3x^3 - x^2 + 8 - 2x^2 - 3x - 1$$

$$3x^3 - 3x^2 - 3x + 7$$

Find the difference of the given polynomials. Represent your final answer in standard form.

2)  $(7y^2 + 9y) - (3y^2 + 7)$

$$7y^2 + 9y - 3y^2 - 7$$

$$4y^2 + 9y - 7$$

3) Subtract  $(5x^2 - 2x + 1)$  from  $x^2 + 5x$   
comes first

$$x^2 + 5x - (5x^2 - 2x + 1)$$

$$x^2 + 5x - 5x^2 + 2x - 1$$

$$-4x^2 + 7x - 1$$



### NOW IT'S YOUR TURN

4)  $(6x^3 + 7x) - (3x^2 + 5) + (x^2 - 10x - 1)$

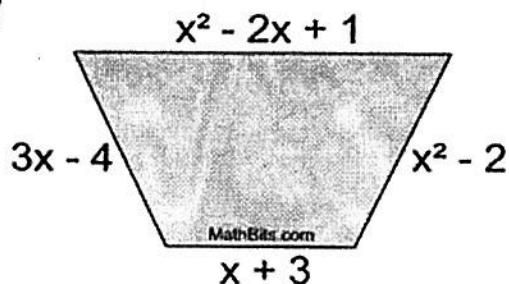
$$6x^3 + 7x - 3x^2 - 5 + x^2 - 10x - 1$$

$$6x^3 - 2x^2 - 3x - 6$$

5) Write a simplified polynomial expression that represents the perimeter of the quadrilateral.

$$3x - 4 + x^2 - 2x + 1 + x^2 - 2 + x + 3$$

$$2x^2 + 2x - 2 \quad \text{units}$$



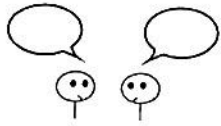
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**TAKEAWAY**

We can add and subtract polynomials by combining like terms.

**Reminder:** Always distribute the - sign when subtracting.

Turn and Talk:



- 1) Is it possible that a sum of two binomials results in a monomial? Justify your response with an example.

Yes, when you have additive inverses

$$\text{ex. } (6x+5) + (3x-5)$$

$$9x$$

- 2) The RMS Spotlight club is sponsoring a school dance with complimentary refreshments in order to fundraise for their upcoming show. They have made a list of expenses and revenue. Using the list, write a simplified polynomial expression in standard form that represents their profit if  $x$  students attend the dance.

Revenue	Expenses
Admission Fee - \$5.00 per student	DJ - \$500
PFA Donation - \$200	Refreshments per student - \$1.50

$x$ : number of students who attend the dance

$$\text{profit} = \text{revenue} - (\text{expenses})$$

$$= 5x + 200 - (1.50x + 500)$$

$$= 5x + 200 - 1.5x - 500$$

$$\longrightarrow \boxed{3.5x - 300}$$

Using your expression, calculate the profit of the club if 620 students attend the dance.

$$p = 3.5x - 300$$

$$= 3.5(620) - 300$$

$$= 2170 - 300$$

$$= \$1870$$