

Solve each system algebraically and check your solution.

$$1. \begin{cases} y = 3x \\ 5x + 2y = 44 \end{cases}$$

$$5x + 2(3x) = 44$$

$$5x + 6x = 44$$

$$11x = 44$$

$$\boxed{x = 4}$$

$$y = 3x$$

$$y = 3(4)$$

$$\boxed{y = 12}$$

check (4, 12)

$$\begin{array}{l} y = 3x \\ 12 = 3(4) \\ 12 = 12 \\ \checkmark \end{array} \quad \begin{array}{l} 5x + 2y = 44 \\ 5(4) + 2(12) = 44 \\ 20 + 24 = 44 \\ 44 = 44 \\ \checkmark \end{array}$$

$$2. \begin{cases} x = 5y - 1 \\ x + 2y = 13 \end{cases}$$

$$5y - 1 + 2y = 13$$

$$7y - 1 = 13$$

$$7y = 14$$

$$\boxed{y = 2}$$

$$x = 5y - 1$$

$$x = 5(2) - 1$$

$$\boxed{x = 9}$$

check (9, 2)

$$\begin{array}{l} x = 5y - 1 \\ 9 = 5(2) - 1 \\ 9 = 10 - 1 \\ 9 = 9 \\ \checkmark \end{array} \quad \begin{array}{l} x + 2y = 13 \\ 9 + 2(2) = 13 \\ 9 + 4 = 13 \\ 13 = 13 \\ \checkmark \end{array}$$

$$3. \begin{cases} -3x + y = 7 \\ 5x + 2y = 3 \end{cases} \rightarrow y = 3x + 7$$

$$5x + 2y = 3$$

$$5x + 2(3x + 7) = 3$$

$$5x + 6x + 14 = 3$$

$$11x + 14 = 3$$

$$11x = -11$$

$$\boxed{x = -1}$$

$$-3x + y = 7$$

$$-3(-1) + y = 7$$

$$3 + y = 7$$

$$\boxed{y = 4}$$

check (-1, 4)

$$\begin{array}{l} -3x + y = 7 \\ -3(-1) + 4 = 7 \\ 3 + 4 = 7 \\ 7 = 7 \end{array} \quad \begin{array}{l} 5x + 2y = 3 \\ 5(-1) + 2(4) = 3 \\ -5 + 8 = 3 \\ 3 = 3 \\ \checkmark \end{array}$$

4. Kasey sells athletic shoes at a department store. She earns \$500 per month plus a 4% commission on her total sales. Kyle also sells athletic shoes at the same store but he earns \$400 per month plus a 5% commission on total sales.

- a. Write a system of equations that represent the total earnings of Kasey and Kyle in one month. Let x represent the amount of money generated in sales and let y represent the total amount of money earned. [Hint: Percents need to be changed to decimals.]

$$\text{Kasey } (y) = 500 + .04x$$

$$\text{Kyle } (y) = 400 + .05x$$

$$500 + .04x = 400 + .05x$$

$$100 + .04x = .05x$$

$$\frac{100}{.01} = \frac{.01x}{.01}$$

$$10,000 = x$$

$$y = 400 + .05x$$

$$y = 400 + .05(10,000)$$

$$y = 400 + 500$$

$$y = 900$$

- b. Solve the system algebraically. What is the solution? What does it mean in the context of the problem?

$$(10,000, 900)$$

\nearrow sales \nearrow \$ earned

Both Kasey and Kyle will: earn the same amount of money (\$900) when they each sell \$10,000 worth of athletic shoes.