## Important Terminology

Natural
Square Roo $\dagger$
Property
Distributive

Whole
Cube Root
Commutative
Equivalent

Integer
Radical
Associative

Rational
Index
Inverse

Irrational
Radicand
Identity

What should I be able to do?

1. Classify numbers using all the subgroups of real numbers (natural, whole, integer, rational, irrational)
2. Determine if the sum or product of two rational numbers is rational or irrational.
3. Determine if the sum or product of two irrational numbers is rational or irrational.
4. Determine if the sum or product of a rational number and an irrational number is rational or irrational.
5. Identify the properties of real numbers.
6. Determine if expressions are equivalent using the properties of real numbers.
7. Rewrite square root radical expressions in simplest radical form.

## Practice Problem Set

1. Using the words natural, whole, integer, rational and irrational, list all the subsets of real numbers to which each number belongs.
a) 115
b) 29.2
c) $\sqrt{10}$
d) $\sqrt[3]{-27}$ $\qquad$
2. Write two numbers that fit each description. If there is no such number, write none.
a) negative integer
b) negative rational number that is not an integer $\qquad$
c) irrational integer $\qquad$
d) negative irrational number $\qquad$

True/False. If false, explain why the statement is false.
3. $-\sqrt{25}$ is a rational number. $\qquad$
4. $\sqrt[3]{9}$ is a rational number. $\qquad$
5. The sum of two irrational numbers is always an irrational number. $\qquad$
6. The product of two irrational numbers is always an irrational number. $\qquad$
7. State whether the numbers below are rational or irrational.
a) $\sqrt{144}$
b) $\sqrt[3]{-64}$
c) $\sqrt{30}$
d) $\sqrt[3]{18}$
8. Rewrite each square root radical in simplest radical form.
a) $\sqrt{24}$
b) $\sqrt{32}$
c) $\sqrt{63}$
d) $\sqrt{108}$

Identify the property shown by the statement below.
9. $14+-15=-15+14$
10. $x y+x z=x(y+z)$
11. $a+0=a$
12. $b \cdot \frac{1}{b}=1$
13. $-2+(5+1)=(-2+5)+1$
14. $(-3)(4)=(4)(-3)$
15. $x+-x=0$
16. $3.5 \cdot(2 \cdot 1.2)=(3.5 \cdot 2) \cdot 1.2$
17. $8 \bullet 1=8$

## Multiple Choice

18. If $S$ is a non-zero rational number and $T$ is an irrational number, which expression(s) will always result in an irrational number?
I. $\quad S+T$
II. ST
III. $\mathrm{T}^{2}$
(1) I
(2) II
(3) I and II only
(4) I, II and III
19. Which set of numbers best describes the different amounts of ingredients that are possible to use in a recipe?
(1) whole numbers
(2) positive rational numbers
(3) integers
(4) real numbers

## Extended Response

20. Ernie says that it's possible for the product of two irrational numbers to be rational. State whether or not you agree with Ernie. Provide mathematical evidence to support your statement.
21. The process of showing that $2 x+3 x$ is equivalent to $5 x$ is shown below. Identify the property used in each step.

Step 1: $2 x+3 x \quad$ Given expression
Step 2: $\times(2+3)$
Step 3: $x(5) \quad$ Combine terms
Step 4: $5 x$
The steps above prove that the expression $2 x+3 x$ is the same as $5 x$. Prove the equivalence of these two expressions in another way.
22. The following flow diagram shows that $a(b c)$ is equivalent to $b(a c)$.

Fill in each circle with the appropriate symbol that represents the property used to form the equivalent expression.
$\mathrm{C}_{X}=$ commutative property of multiplication
$\mathrm{A}_{X}=$ associative property of multiplication


