Essential Questions: What is a system of linear equations? How can we solve a linear system graphically?

## Do Now:

a) On the same set of axes, graph the following lines.

$$
y=-2 x+4 \quad y=x-2
$$


b) At which point do the lines intersect? $\qquad$ y

## What is a System of Linear Equations?

- A system of linear equations, also called a linear system, consists of two or more linear equations that have the same variables.
- A solution of a system of linear equations with two variables is an ordered pair that satisfies all of the equations in the system. The values of the variables in the ordered pair make each equation in the system true.
- When graphing, you will encounter three possible solution sets.

Intersecting Lines

$\qquad$ solution

Parallel Lines

$\qquad$ solution

Coinciding Lines

$\qquad$ solutions

Parallel lines have the $\qquad$ slope and $\qquad$ $y$-intercepts.

Coinciding lines have the $\qquad$ slope and $\qquad$ $y$-intercepts.

1) What is the solution of the system graphed below?

2) Find the solution to the following system:
$-3 x+3 y=9$

$$
2 x+y=6
$$

1. $(2,-2)$
2. $(-2,2)$
3. No solution
4. Infinitely many solutions


## Calculator Check:

1) Input both equations into $y=$
2) $2^{\text {nd }}$ Trace (Calc)
3) \#5 intersect
4) Press Enter 3 times

Also check the table of values
3) One family fitness center has a $\$ 50$ enrollment fee and costs $\$ 30$ per month. Another center has no enrollment fee but costs $\$ 40$ per month. Write an equation for each payment option. Let $T$ represent the total amount paid to the fitness center and let $m$ represent the number of months the fitness center is used.

Equation (Option 1): $\qquad$
Equation (Option 2): $\qquad$
a. Graph both cost equations over a 10 month period.

| $X$ <br> (months) | $Y$ <br> (opt. 1) | $\mathbf{Y}$ <br> (opt. 2) |
| :---: | :---: | :---: |
| 0 |  |  |
| 1 |  |  |
| 2 |  |  |
| 3 |  |  |
| 4 |  |  |
| 5 |  |  |
| 6 |  |  |
| 7 |  |  |
| 8 |  |  |
| 9 |  |  |
| 10 |  |  |


b. In how many months will both fitness centers cost the same?

## The ${ }^{\text {The }}$ AWEAY

To solve a linear system graphically, graph each $\qquad$ Identify the point of $\qquad$ . Check the solution with $\qquad$ equations.

Checks can be done algebraically or using a graphing calculator. Linear systems have 3 possible solution sets: $\qquad$ solution, $\qquad$ solution or $\qquad$ solutions.

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Solve the following systems of equations graphically and check. If no solution exists, no check is required.

1. $x+y=-3$
$2 x=-4-2 y$

2. $x+y=-2$

$$
y=\frac{1}{3} x+2
$$


3. Your family starts a bed-and-breakfast. They spend $\$ 500$ fixing up a bedroom to rent. The costs for food and utilities is $\$ 10$ per night. Your family charges $\$ 60$ per night to rent the bedroom. The equation that represents the costs to your family is $\mathbf{y}=\mathbf{1 0 x + 5 0 0}$ where $\mathbf{x}$ represents the number of nights the room is rented. The equation that represents the revenue (income) for your family is $\mathbf{y}=\mathbf{6 0 x}$ where $\mathbf{x}$ represents the number of nights the room is rented.
a) Use the cost and revenue equations to complete the table below.

| $x$ (number of nights) | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cost |  |  |  |  |  |  |  |  |  |  |  |  |
| Revenue |  |  |  |  |  |  |  |  |  |  |  |  |

b) Graph the system.

c) State the point of intersection. What does this point tell us in the context of the situation?

