

Algebra RH

Essential Question: What are literal equations?

Do Now: Solve for x.

$$x + a = b$$

$$-a \quad -a$$

$$x = b - a$$

to check
 substitute numbers in each equation and see if they are equal in value
 $x=1$
 $a=2$
 $b=3$
 $x+a=b$
 $1+2=3$
 $x=b-a$
 $1=3-2$
 of substitute answer for x in original equation $(b-a)+a=b$
 $b=b$

The properties of equality justify the series of inverse operations that are performed in order to solve an equation.

Addition Property of Equality	If $a = b$, then $a + c = b + c$
Subtraction Property of Equality	If $a = b$, then $a - c = b - c$
Multiplication Property of Equality	If $a = b$, then $ac = bc$
Division Property of Equality	If $a = b$, then $\frac{a}{c} = \frac{b}{c}, c \neq 0$

Example:

Write the property of equality used in each step in solving the equation.

Steps	Property
$-5x - 4 = 16$	
$-5x = 20$	addition property of equality
$x = -4$	division property of equality

Literal Equations: an equation with two or more distinct variables

When solving for another variable in an equation:

- Ask yourself, "What happened to the variable being solved?"
- Keep in mind, the last operation done is the first undone using inverse operations.
- Always keep your equation balanced (what you do to one side must be done to the other side).

Examples: Solve for x.

1. $\frac{ax}{a} = \frac{b}{a}$

$$x = \frac{b}{a}$$

2. $a \left(\frac{x}{a} \right) = (b) a$

$$x = ba$$

3. $\frac{x}{a} + c = d$

$$-c \quad -c$$

$$a \left(\frac{x}{a} \right) = (d - c) a$$

$$x = a(d - c)$$

$$4. \frac{a(x-4)}{a} = \frac{b}{a}$$

$$x-4 = \frac{b}{a}$$

$$+4 \quad +4$$

$$x = \frac{b}{a} + 4$$

$$7. c = 3x - 3b$$

$$+3b \quad +3b$$

$$\frac{c+3b}{3} = \frac{3x}{3}$$

$$\frac{c+3b}{3} = x \quad \text{or} \quad \frac{c}{3} + b = x$$

Solve for the variable indicated.

$$10. C = \frac{5}{9}(F-32); F$$

eliminate fractional
co-efficient by
multiplying by its
reciprocal

$$\frac{9}{5}C = F-32$$

$$\frac{9}{5}C + 32 = F$$

$$5. \frac{x}{a-b} = \frac{c}{1}$$

$$x = c(a-b)$$

$$*8. c - 2x = bx$$

get variables that are
the same to the same
side

$$c = bx + 2x$$

factor out variable

$$\frac{c}{b+2} = x \left(\frac{b+2}{b+2} \right)$$

$$11. A = \frac{1}{2}h(b_1+b_2); h$$

$$\frac{2A}{(b_1+b_2)} = h \left(\frac{b_1+b_2}{(b_1+b_2)} \right)$$

$$\frac{2A}{(b_1+b_2)} = h$$

$$6. \frac{a}{(x-b)} = \frac{c}{d}$$

$$ad = c(x-b)$$

$$\frac{ad}{c} = x-b$$

$$\frac{ad}{c} + b = x$$

$$*9. a = \frac{1}{3}(b+x)$$

eliminate fractional
co-efficient first,
if possible

$$3a = b+x$$

$$-b \quad -b$$

$$3a-b = x$$

$$\frac{c}{b+2} = x$$

$$12. P = 2(l+w); w$$

either

$$\frac{P}{2} = l+w$$

$$-l \quad -l$$

$$\frac{P}{2} - l = w$$

or

$$P = 2l + 2w$$

$$\frac{P-2l}{2} = \frac{2w}{2}$$

$$\frac{P-2l}{2} = w$$

$$\frac{P}{2} - l = w$$