## Algebra RH

Essential Question: How do we recognize what type of regression equation can be used to model data?

Do Now:
The following data shows the number of species of mammals on the International Union for Conservation of Nature's "Red List" of endangered species during the years 2004 to 2012.

| Year | 2004 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Species | 352 | 348 | 349 | 448 | 449 | 450 | 447 | 446 |

a) Using a linear regression model, find the equation of the line of best fit.
b) Using your equation, how many species are expected to be in danger in 2016 ?

The data from a scatterplot can form a shape that indicates what type of equation should be used to approximate the relationship between the two variables.

## Choosing a Linear, Quadratic, and Exponential Model

$$
\begin{array}{ccc}
\text { Linear } & \text { Quadratic } & \text { Exponential } \\
y=m x^{\prime}+b & y=a x^{2}+b x+c & y=a b^{x}
\end{array}
$$



Once you view the scatterplot of a graph, you can determine what model best approximates the data. If a set of data takes on the shape of an exponential growth or decay, use an exponential regression equation for the data set. See graph below.


## Calculator Corner

Remember, in order to create a scatterplot:

1) $\operatorname{STAT} \operatorname{PLOT}\left(2^{\text {nd }} y=\right) \# 1$ ENTER
2) Turn On and Choose Scatter Plot
3) Use STAT EDIT to enter data into $\mathrm{L}_{1}$ and $\mathrm{L}_{2}$

4) ZOOM \#9 (ZOOM STAT) [view the graph and decide which model to use]

To create the equation for your function:
STAT $\rightarrow$ CALC
\#4 LinReg (linear)
\#5 QuadReg (quadratic)
\#0 ExpReg (exponential)

## Examples:

1. A population of single-celled organisms was grown in a Petri dish over a period of 16 hours. The number of organisms at a given time is recorded in the table below.

| Time (hrs) | $\boldsymbol{x}$ | 0 | 2 | 4 | 6 | 8 | 10 | 12 | 16 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Number of <br> Organisms | $\boldsymbol{y}$ | 25 | 36 | 52 | 68 | 85 | 104 | 142 | 260 |

a) Determine the exponential regression equation model for these data, rounding all values to the nearest ten-thousandth.
b) Using this equation, predict the number of single-celled organisms, to the nearest whole number, at the end of the 18th hour.
2. About a year ago, Joey watched an online video of a band and noticed that it had been viewed only 843 times. One month later, Joey noticed that the band's video had 1708 views. Joey made the table below to keep track of the cumulative number of views the video was getting online.

| Months Since <br> First Viewing | Total Views |
| :---: | :---: |
| 0 | 843 |
| 1 | 1708 |
| 2 | forgot to record |
| 3 | 7124 |
| 4 | 14,684 |
| 5 | 29,787 |
| 6 | 62,381 |

a) Write a regression equation that best models these data. Round all values to the nearest hundredth. Justify your choice of regression equation.
b) As shown in the table, Joey forgot to record the number of views after the second month. Use the equation from part a to estimate the number of full views of the online video that Joey forgot to record.
3. Biologists conducted a study of the nesting behavior of a type of bird called a flycatcher. They examined a large number of nests and recorded the latitude for the location of the nest and the number of chicks in the nest.

a) What type of model (linear, quadratic or exponential) would best describe the relationship between latitude and mean number of chicks?
b) One model that could be used to describe the relationship between mean number of chicks and latitude is $\boldsymbol{y}=\mathbf{0 . 1 7 5 + 0 . 2 1 x} \mathbf{- 0 . 0 0 2} \boldsymbol{x}^{\mathbf{2}}$, where $\boldsymbol{x}$ represents the latitude of the location of the nest and $\boldsymbol{y}$ represents the number of chicks in the nest.

Use the quadratic model to complete the following table.

| $\boldsymbol{x}$ <br> Latitude | 30 | 40 | 50 | 60 | 70 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ <br> Mean Number of <br> Chicks |  |  |  |  |  |

c) Based on this quadratic model, what is the best latitude for hatching the most flycatcher chicks? Justify your response.

## TAKE AWAY

Models can be used to answer questions about how two variables are related (bivariate data).
$\qquad$ , $\qquad$ and $\qquad$ equations are common models that can be used to describe the relationship between two variables.

