8 Algebra CC 15-3

**Essential Questions:** How do we determine the domain and range of a quadratic function? How do we determine when the function is increasing? How do we determine when the function is decreasing?

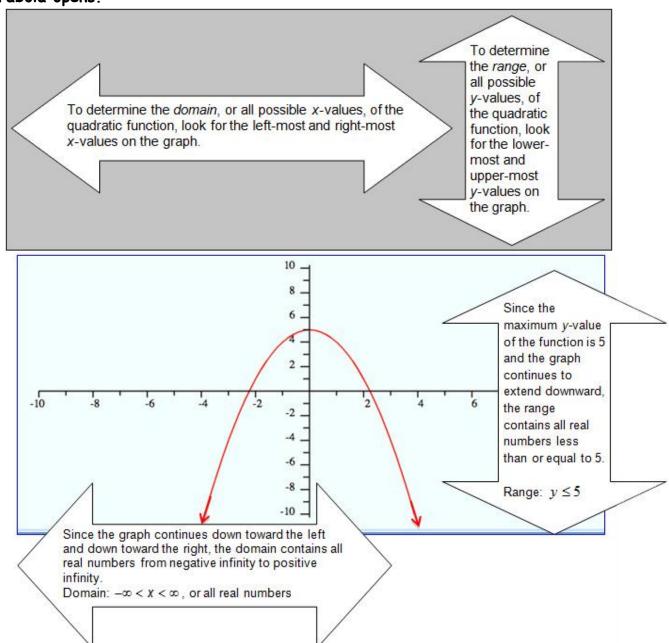
Do Now: Complete the table with the correct terminology.

| output |
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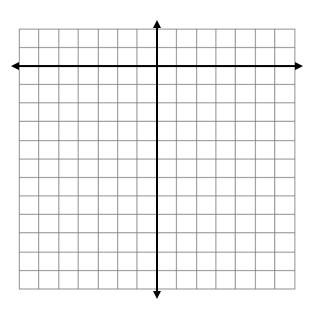
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## **Domain and Range of Quadratic Functions**

Substituting any real value of x into a quadratic equation results in a real number. Therefore, in general, the <u>domain</u> of any quadratic function is <u>all</u> real numbers. The <u>range</u> of a quadratic function depends on its <u>vertex</u> and the <u>direction</u> that the parabola opens.



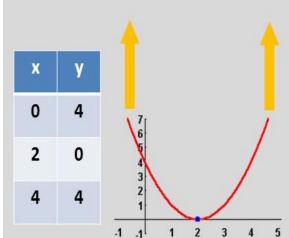
- 1) Graph the quadratic function  $y = -x^2 + 4x 6$ State the:
  - Vertex: \_\_\_\_\_\_
  - Maximum or minimum\_\_\_\_\_\_\_
  - *x*-intercepts: \_\_\_\_\_
  - Zeros (roots): \_\_\_\_\_
  - Domain: \_\_\_\_\_
  - Range: \_\_\_\_\_

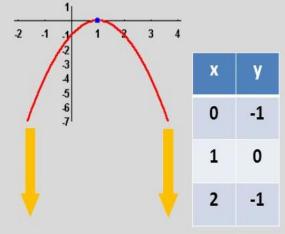


## **Behavior of a Quadratic Function**

Given a quadratic function in the form of  $f(x) = ax^2 + bx + c$ 

| a > 0   | a < 0   |
|---|---|
| <ul> <li>Opens up</li> </ul>                  | <ul> <li>Opens down</li> </ul>                |
| <ul> <li>Vertex is a minimum point</li> </ul> | <ul> <li>Vertex is a maximum point</li> </ul> |
| <ul> <li>ends approach ∞</li> </ul>           | <ul> <li>ends approach -∞</li> </ul>          |

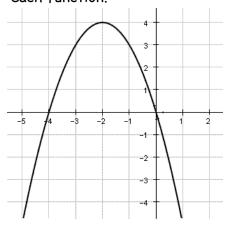


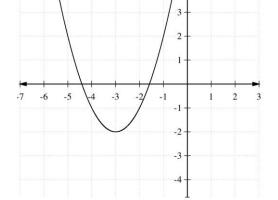


- The function is *decreasing* for all values in which x < 2</li>
- The function is *increasing* for all values in which x > 2
- The ends of the graph approach + ∞

- The function is *increasing* for all values in which x < 1</li>
- The function is *decreasing* for all values in which x > 1
- The ends of the graph approach ∞

2) Describe the end behavior of the following graphs. Describe the intervals for which the functions are increasing and the intervals for which they are decreasing. State the range of each function.





End behavior:

Increasing: \_\_\_\_\_

End behavior:

Increasing: \_\_\_\_\_

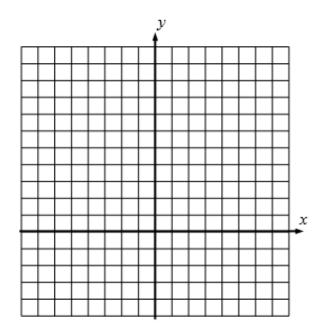
Decreasing: \_\_\_\_\_

Decreasing:

Range:

- 3) Consider the quadratic function  $f(x) = x^2 + 4x 1$ 
  - (a) Graph the function.

Range: \_\_\_\_\_



(b) State the range of the function.

(c) State the interval over which f(x) is increasing.