Algebra RH
Essential Question: How can we determine the average rate of change of an exponential function over a specific interval?

Do Now: Consider the exponential function, $f(x)=8(2)^{x}$.
a) Evaluate f(3).
b) What ordered pair would lie on the graph of $f(x)$ based on $f(3)$ ?


Let's take a closer look at exponential functions.

Make a table of values and graph the following exponential functions over the given interval.

1. $G r a p h ~ f(x)=(2.5)^{x}$ over the interval $0 \leq x \leq 3$

| $\mathbf{x}$ | $\mathbf{f ( x )}$ |
| :--- | :--- |
|  |  |
|  |  |
|  |  |
|  |  |



What is the average rate of change of the function over the interval?

Interval begins at: $\qquad$ Average Rate of Change:

Interval ends at: $\qquad$
2. Consider the exponential function $f(x)=10(2)^{x}$.
a) Find the value of $f(0)$. What point does this represent on the graph?
b) Is this an increasing or decreasing exponential function? How do you know?
c) Using your calculator, sketch a graph of this function on the axes shown below. Use the window indicated. Mark the $y$-intercept.

d) What is the function's average rate of change over the interval $-1 \leq x \leq 2$ ?
e) Is this rate of change greater than or less than that of the linear function $g(x)=10 x+7$ ? Explain.

Exponential functions are curves that either increase or decrease rapidly. We can determine an average $\qquad$ of a specific part of an exponential function by using two points that mark the beginning and end of the $\qquad$ by calculating $\frac{\Delta y}{\Delta x}$.
$\qquad$

1. Classify each of the following exponential functions as either increasing or decreasing and give the value of their $y$-intercepts.
a) $f(x)=125(1.25)^{x}$
b) $f(x)=22(0.75)^{x}$
c) $f(x)=256\left(\frac{5}{2}\right)^{x}$
2. Which of the following could be the equation to the exponential function graphed below? Explain how you made your choice.
(1) $y=15(1.25)^{x}$
(2) $y=50(1.04)^{x}$
(3) $y=18(0.75)^{x}$
(4) $y=40(0.45)^{x}$

3. Using your graphing calculator, create a table of values and draw a sketch of the exponential function $y=3(2.5)^{x}$ over the interval $-4 \leq x \leq 4$. Use the window indicated.


What is the average rate of change of the function over the given interval?
4. Which of the following is a decreasing exponential function whose $y$-intercept is 20 ?
(1) $y=20\left(\frac{4}{3}\right)^{x}$
(2) $y=-2 x+20$
(3) $y=20\left(\frac{1}{3}\right)^{x}$
(4) $y=\left(\frac{1}{3}\right)^{x}+20$
5. Which of the following functions would best describe the data in the table?
(1) $y=10 x+2$
(2) $y=8 x+2$
(3) $y=5(2)^{x}$
(4) $y=2(5)^{x}$

| $x$ | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 2 | 10 | 50 | 250 | 1250 |

