

Algebra RH

Essential Question: What is function notation? How do we represent functions using function notation?

Do Now:

A function can be written in function form by replacing the “y” with “f(x)” read as “f of x.”

Example:

- $y = 3x + 1$ is a linear function. $y = 3x + 1$ written in function notation is $f(x) = 3x + 1$.
- $y = 3x + 1$ can also be written as $g(x) = 3x + 1$ or $h(a) = 3a + 1$
- The solutions to $y = 3x + 1$ are (x, y) , for $f(x) = 3x + 1$ the solutions are $(x, f(x))$

Make a table of values for $f(x) = 3x + 1$ using the domain $\{0,1,2,3\}$.

$f(x) = 3x + 1$

x	f(x)
0	1
1	4
2	7
3	10

Representing Functions Using Function Notation



Think about this:

Since not every equation in two variables is a function, we use function notation to describe functions.

$y = 2x + 3$ written in function notation is $f(x) = 2x + 3$.

Input x	Function Rule $f(x) = 2x + 3$	Output f(x)	Ordered Pairs (x, f(x))
-3	$f(-3) = 2(-3) + 3$	-3	$(-3, -3)$
4	$f(4) = 2(4) + 3$	11	$(4, 11)$
7	$f(7) = 2(7) + 3$	17	$(7, 17)$

More Functions

1. Given the following functions, answer each question

$$f(x) = \frac{x-6}{2}$$

$$g(x) = \sqrt{2x+1}$$

$$h(x) = \frac{x}{3} + 7$$

$$a(x) = x^2 + 2x - 1$$

$$\begin{aligned} \text{a) } f(2) &= \frac{2-6}{2} \\ &= \frac{-4}{2} \\ &= -2 \end{aligned}$$

$$\begin{aligned} \text{b) } g(4) &= \frac{\sqrt{2(4)+1}}{\sqrt{9}} \\ &= \frac{3}{3} \end{aligned}$$

$$\begin{aligned} \text{c) } a(2) &= (2)^2 + 2(2) - 1 \\ &= 7 \end{aligned}$$

$$\begin{aligned} \text{d) } h(-9) &= \frac{-9}{3} + 7 \\ &= -3 + 7 \\ &= 4 \end{aligned}$$

$$\begin{aligned} \text{e) } f(3) &= \frac{3-6}{2} \\ &= \frac{-3}{2} \end{aligned}$$

$$\begin{aligned} \text{f) } g\left(\frac{19}{2}\right) &= \sqrt{2\left(\frac{19}{2}\right)+1} \\ &= \sqrt{20} \\ &= \sqrt{4} \sqrt{5} \\ &= 2\sqrt{5} \end{aligned}$$

$$\text{g) } f(a+1) =$$

$$\begin{aligned} &\frac{a+1-6}{2} \\ &= \frac{a-5}{2} \end{aligned}$$

$$\text{h) } g(-13) =$$

$$\begin{aligned} &\sqrt{2(-13)+1} \\ &= \sqrt{-25} \\ &= 5i \end{aligned}$$

$$\text{i) } a(-4) =$$

$$\begin{aligned} &(-4)^2 + 2(-4) - 1 \\ &= 7 \end{aligned}$$

$$\text{j) } a(x-3) =$$

$$\begin{aligned} &(x-3)^2 + 2(x-3) - 1 \\ &= x^2 - 6x + 9 + 2x - 6 - 1 \\ &= x^2 - 4x + 2 \end{aligned}$$

$$\text{k) } h(-6a) = \frac{-6a}{3} + 7$$

$$= -2a + 7$$

$$\text{l) Solve for } x \text{ if } f(x) = 13$$

$$\begin{aligned} 13 &= \frac{x-6}{2} \\ 26 &= x-6 \\ 32 &= x \end{aligned}$$

$$\text{m) Solve for } x \text{ if } h(x) = -2$$

$$\begin{aligned} -2 &= \frac{x}{3} + 7 \\ -9 &= \frac{x}{3} \end{aligned}$$

$$\text{n) If } b(x) = 2f(x) - 1 \text{ then what is } b(6)?$$

$$\begin{aligned} &= 2f(6) - 1 \\ &= 2\left(\frac{6-6}{2}\right) - 1 \\ &= 2\left(\frac{0}{2}\right) - 1 = -1 \end{aligned}$$

OR $b(x) = \frac{2(x-6)}{2} - 1$

$$\begin{aligned} b(x) &= x - 6 - 1 \\ b(x) &= x - 7 \\ b(6) &= 6 - 7 \end{aligned}$$

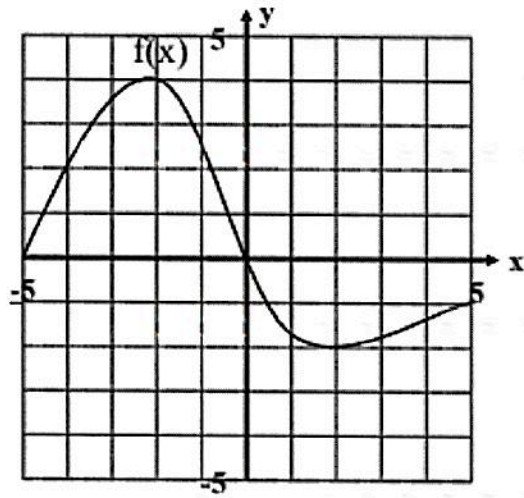
$$x = -27$$

2. Find the range of the function $h(x) = 2x - 5$ when the domain = $\{-1, 0, 1, 2, 3\}$.

x	h(x)
-1	-7
0	-5
1	-3
2	-1
3	1

3. Using the graph to the right of $f(x)$

- $f(2) = -2$
- $f(0) = 0$
- $f(-4) = 2$
- Find x if $f(x) = -2$ $x = 2$
- Find x if $f(x) = 0$ $x = -5, 0$
 $\{-5, 0\}$



4. Given the functions $h(x) = -3(x + 1)$ and $g(x) = x^2 - 5$

- Evaluate $h(2) + g(-1)$

$$\begin{array}{r} -3(2+1) + (-1)^2 - 5 \\ -9 + -4 = -13 \end{array}$$
- Find $h(x) + g(x)$ in standard form

$$\begin{array}{r} -3(x+1) + x^2 - 5 \\ -3x - 3 + x^2 - 5 \rightarrow x^2 - 3x - 8 \end{array}$$
- Find $h(2a) + g(a)$

$$\begin{array}{r} -3(2a+1) + (a)^2 - 5 \\ -6a - 3 + a^2 - 5 \rightarrow a^2 - 6a - 8 \end{array}$$
- True or False? $g(2.5) < h(-1.5)$

$$\begin{array}{r} (2.5)^2 - 5 < -3(-1.5 + 1) \\ 6.25 - 5 < -3(-.5) \\ 1.25 < 1.5 \quad \text{True} \end{array}$$