

Essential Question: What types of numbers result from multiplying rational and irrational numbers?

Do Now: Determine if each statement is true or false. Use the order of operations to evaluate each side of the equation.

a) $\sqrt{4} \cdot \sqrt{9} = \sqrt{36}$

b) $5 \cdot 3\sqrt{4} = 15\sqrt{4}$

c) $6\sqrt{9} \cdot 2\sqrt{4} = 12\sqrt{36}$



How do we multiply radical expressions?

Rule: $a\sqrt{b} \cdot c\sqrt{d} = ac\sqrt{bd}$

1st: Multiply Coefficients

2nd: Multiply Radicands

Never multiply a coefficient and a radicand

Multiply the radical expressions below. Simplify if possible.

1) $\sqrt{2} \cdot \sqrt{5}$

2) $\sqrt{3} \cdot \sqrt{15}$

3) $6\sqrt{7} \cdot 4\sqrt{2}$

What type of number is the result of the product of two rational numbers?

a) 5×10

b) $\frac{1}{2} \times \frac{5}{9}$

c) $-8.\bar{2} \times 0$

d) $\sqrt{4} \times \sqrt{25}$

Conclusion:

The **product** of two **rational** numbers is always a _____ number.

What type of number is the result of the product of a rational number and an irrational number?

a) $6 \times \sqrt{2}$

b) $\pi \times 100$

c) $\sqrt{4} \times \sqrt{5}$

d) $0 \times \sqrt{18}$

Conclusion:

The **product** of a **non-zero rational** number and an **irrational** number is always an _____ number.

What type of number is the result of the product of two irrational numbers?

a) $\pi \times \pi$

b) $\sqrt{2} \times \sqrt{5}$

c) $\sqrt{2} \times \sqrt{8}$

d) $(\sqrt{7})^2$

e) $\pi \times \frac{1}{\pi}$

Conclusion:

The **product** of **two irrational** numbers can result in a _____ number or an _____ number.

Remember:

$R \bullet R = \underline{\hspace{2cm}}$

$I \bullet R = \underline{\hspace{2cm}}$ ($R \neq 0$)

$I \bullet I = \underline{\hspace{2cm}}$

The
TAKEAWAY

Sums and Products of Rational and Irrational Numbers

- Addition of two rational numbers will result in a sum that is a(n) _____ number.
- Multiplication of two rational numbers will result in a product that is a(n) _____ number.
- Addition of a rational number and an irrational number will result in a(n) _____ sum.
- Multiplication of a non-zero rational number and an irrational number results in a(n) _____ product.
- The sum or product of two irrational numbers may be _____ or _____.

PROPERTIES OF REAL NUMBERS

Property	Example
Commutative Property of Addition $A + B = B + A$	
Commutative Property of Multiplication $AB = BA$	
Associative Property of Addition $(A + B) + C = A + (B + C)$	$6 + 3 + 7$ $6 + 3 + 7$
Associative Property of Multiplication $(A \times B) \times C = A \times (B \times C)$	$-4 \cdot 2 \cdot 5$ $-4 \cdot 2 \cdot 5$

Property	Example
<p>Identity Property of Addition</p> $A + \quad = A$	
<p>Identity Property of Multiplication</p> $A \times \quad = A$	
<p>Inverse Property of Addition</p> $A + (-A) =$	<p>*Additive Inverse means <u>OPPOSITE</u></p>
<p>Inverse Property of Multiplication</p> $A \times (1/A) =$	<p>*Multiplicative Inverse means <u>RECIPROCAL</u></p>
<p>Distributive Property</p> $A(B + C) = AB + AC$ <p style="text-align: center;">or</p> $A(B - C) = AB - AC$	$3(2 + 8)$ $3(4 - y)$

IT'S TIME TO TEST YOUR KNOWLEDGE...

	$x + 0 = x$
	$-3(7) = 7(-3)$
	$6(y + z) = 6y + 6z$
	$(-2 \cdot 10) \cdot -7 = -2 \cdot (10 \cdot -7)$
	$\frac{1}{4} (4) = 1$
	$\frac{2}{5} \cdot \frac{3}{3} = \frac{6}{15}$