Essential Question: What types of numbers result from adding and multiplying rational and irrational numbers?

Do Now:

- 1) Add the following pairs of rational numbers.
- a) $\frac{2}{3} + \frac{5}{9}$

- b) $6+19.\overline{3}$ c) $-\sqrt{49}+\sqrt{121}$
- d) $\sqrt[3]{8} + \frac{1}{2}$

Adding Rational Numbers

_number. The sum of two rational numbers will always be a _____

Adding Irrational Numbers

How do we add irrational numbers?



Note: When adding radical expressions, the radicands must be the same in order to combine the terms.

Examples: a) $\sqrt{5} + 3\sqrt{5} = 4\sqrt{5}$ b) $2\sqrt{7} + 9\sqrt{7} = 11\sqrt{7}$

c) $\sqrt{5} + 2\sqrt{7} = \sqrt{5} + 2\sqrt{7}$

cannot combine terms

a)
$$\pi + \pi$$

b)
$$\sqrt{2} + \sqrt{2}$$
 c) $\sqrt{2} + \sqrt{3}$ d) $\pi + (-\pi)$

c)
$$\sqrt{2} + \sqrt{3}$$

d)
$$\pi + (-\pi)$$

The sum of two irrational numbers may result in an _____ ____ number or number.

Adding Rational and Irrational Numbers

Find the following sums.

a)
$$2+\sqrt{5}$$

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 b) $3+\pi$ c) $-\sqrt{17}+0$

d)
$$\sqrt{25} + \sqrt{54}$$

The sum of a rational number and an irrational number will always be an _ number.

Multiplying Radical Expressions

Rule:
$$a\sqrt{b} \cdot c\sqrt{d} = ac\sqrt{bd}$$

- 1st: Multiply Coefficients 2nd: Multiply Radicands

Never multiply a coefficient and a radicand

Multiply the radical expressions below. Simplify if possible.

1)
$$\sqrt{2} \cdot \sqrt{5}$$

2)
$$\sqrt{3} \cdot \sqrt{15}$$

3)
$$6\sqrt{7} \cdot 4\sqrt{2}$$

What type of number is the result of the product of two rational numbers?

b)
$$\frac{1}{2} \times \frac{5}{9}$$

c)
$$-8.\overline{2} \times 0$$

c)
$$-8.\overline{2} \times 0$$
 d) $\sqrt{4} \times \sqrt{25}$

Conclusion:

The product of two rational numbers is always a _____ number.

What type of number is the result of the product of a rational number and an irrational number?

a)
$$6 \times \sqrt{2}$$

b)
$$\pi \times 100$$

c)
$$\sqrt{4} \times \sqrt{5}$$

d)
$$0 \times \sqrt{18}$$

Conclusion:

The product of a non-zero rational number and an irrational number is always an _____ number.

What type of number is the result of the product of two irrational numbers?

a)
$$\pi \times \pi$$

b)
$$\sqrt{2} \times \sqrt{5}$$

c)
$$\sqrt{2} \times \sqrt{8}$$

d)
$$(\sqrt{7})^2$$

b)
$$\sqrt{2} \times \sqrt{5}$$
 c) $\sqrt{2} \times \sqrt{8}$ d) $(\sqrt{7})^2$ e) $\pi \times \frac{1}{\pi}$

Conclusion:

The product of two irrational numbers can result in a _____ number or an _____ number.