Essential Question: How do we describe relationships using function notation?

Do Now: Read the problem below and complete parts a-c.
A pot of boiling water at 212 degrees Fahrenheit is left in a room that is 65 degrees Fahrenheit. As the water begins to cool, temperature readings are taken each hour and are presented in the table below. In this scenario, the temperature, $\boldsymbol{T}$, is a function of the number of hours, $\boldsymbol{h}$.

| $\boldsymbol{h}$ <br> $(h r s)$ | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\boldsymbol{T}(\boldsymbol{h})$ <br> $\left({ }^{\circ} F\right)$ | 212 | 141 | 104 | 85 | 76 | 70 | 68 | 66 |

(a) Find $\boldsymbol{T}(2)$. What does it mean in the context of the problem?
(b) For what value of $\boldsymbol{h}$ is $\boldsymbol{T}(\boldsymbol{h})=76$ ? What does it mean in the context of the problem?
(c) Examine the table carefully. Do you think the relationship between time and temperature is linear? Be ready to justify your response.

## Describing Relationships Using Function Notation

1. Neal has a $\$ 5$ gift card for music downloads. Each song costs $\$ 1$ to download. The amount of money left on the card, $\boldsymbol{M}$, is a function of the number songs downloaded, $\boldsymbol{x}$.
a) Complete the table below that describes the relationship presented above.

| $\boldsymbol{x}$ | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
| $\boldsymbol{M}(\boldsymbol{x})$ |  |  |  |  |  |  |

b) Is the relationship linear?
c) Sketch a graph of the relationship.

d) Can we write an equation in function notation to represent this scenario?
2. Jenna knits scarves and then sells them on Etsy, an online market place. Let $C(x)=4 x+20$ represent the cost, $\boldsymbol{C}$, in dollars to produce 0 to 6 scarves.
a) Create a table to show the relationship.

| $x$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $c(x)$ |  |  |  |  |  |  |  |

b) What is the meaning of $\boldsymbol{C}(3)$ ?
c) What is the meaning of the solution to the equation $C(x)=40$ ?
3. Next weekend Marnie wants to attend either carnival A or carnival B. Carnival A charges $\$ 6$ for admission and an additional $\$ 1.50$ per ride. Carnival B charges $\$ 2.50$ for admission and an additional $\$ 2$ per ride.
a) In function notation, write a cost equation $\boldsymbol{A}(\boldsymbol{x})$ which represents the total cost of attending carnival $A$ and going on $x$ rides. In function notation, write a cost equation $\boldsymbol{B}(\boldsymbol{x})$ which represents the total cost of attending carnival B and going on $\boldsymbol{x}$ rides.
b) Determine the number of rides Marnie can go on such that the total cost of attending each carnival is the same.
c) Marnie wants to go on five rides. Which carnival should she attend? Justify your response.

## Not all Functions are Linear

4. Physics students throw a ball from the top of a 100 foot building and model its height above the ground as a function of time with the equation $\boldsymbol{h}(\boldsymbol{t})=\mathbf{1 0 0} \mathbf{- 1 6 t} \boldsymbol{t}^{\mathbf{2}}$. The height, $\boldsymbol{h}$, is measured in feet and time, $\boldsymbol{t}$, is measured in seconds.

Find $\boldsymbol{h}(2.5)$. What does this output represent in the context of the problem?


## Partner Activity

You put a yam in the oven. After 45 minutes, you take it out. Let $f(t)$ be the temperature of the yam $\boldsymbol{t}$ minutes after you placed it in the oven.

Explain the meaning of each of the following statements.

| $f(0)=65$ | $f(5)<f(10)$ |
| :--- | :--- |
| $f(40)=f(45)$ | $f(45)>f(60)$ |
|  |  |

