

Algebra RH

Essential Question: How do we evaluate zero and negative exponents?

Do Now: Evaluate.

2^4	2^3	2^2	2^1	2^0	2^{-1}	2^{-2}	2^{-3}
<u>16</u>	<u>8</u>	<u>4</u>	<u>2</u>	<u>1</u>	<u>$\frac{1}{2}$</u>	<u>$\frac{1}{4}$</u>	<u>$\frac{1}{8}$</u>

Important Concepts

a^n ← exponent
↑
base

$$a^0 = 1, a \neq 0$$

any non-zero number raised to the zero power = 1

any expression raised to the negative power moves that expression to the other part of the fraction

$$a^{-n} = \frac{1}{a^n}$$

$$\frac{1}{a^{-n}} = a^n$$

Simplifying Exponential Expressions (express answers with positive exponents)

1. $3^{-2} = \frac{1}{3^2}$

$$\frac{1}{9}$$

4. $\left(\frac{2}{3}\right)^{-2} = \left(\frac{3}{2}\right)^2 \rightarrow \frac{9}{4}$

$$\frac{2^{-2}}{3^{-2}} \rightarrow \frac{3^2}{2^2} = \frac{9}{4}$$

2. $2^{-4} = \frac{1}{2^4}$

$$\frac{1}{16}$$

5. $(5a)^{-1} = \frac{1}{5a}$

3. $a^{-3} = \frac{1}{a^3}$

6. $(-11)^2 y^0 = (-11)(-11)(1) = 121$

7. $x^{-10} y^{21} = \frac{y^{21}}{x^{10}}$

$$8. \ 20x^8y^{-8} \quad \frac{20}{x^8y^8}$$

$$9. \ \frac{1}{3^{-2}} \quad \begin{matrix} 3^2 \\ 9 \end{matrix}$$

$$10. \ \frac{1}{x^{-4}} \quad x^4$$

$$11. \ \frac{6}{18x^{-3}} \quad \frac{1x^3}{3} \rightarrow \frac{x^3}{3}$$

$$12. \ \frac{8^{-2}}{2^{-4}x^{-4}} \quad \frac{2^4x^4}{8^2} \rightarrow \frac{16x^4}{64} \rightarrow \frac{x^4}{4}$$

$$13. \ \frac{x^{-4}}{(12y)^{-2}} \quad \frac{(12y)^2}{x^4} \rightarrow \frac{144y^2}{x^4}$$

$$14. \ \left(\frac{2x}{y^{-1}}\right)^2 \quad (2xy)^2 \rightarrow 2^2x^2y^2 \rightarrow 4x^2y^2$$

$$15. \ \left(\frac{2x}{y^{-1}}\right)^{-2} \quad \begin{matrix} \text{take the} \\ \text{reciprocal} \end{matrix} \quad \left(\frac{y^{-1}}{2x}\right)^2 \quad \left(\frac{1}{2xy}\right)^2 \rightarrow \frac{1}{4x^2y^2}$$

$$\frac{2^{-2}x^{-2}}{y^2} \rightarrow \frac{1}{2^2x^2y^2} \rightarrow \frac{1}{4x^2y^2}$$

$$\text{or } (2xy)^{-2} \rightarrow \frac{1}{(2xy)^2} \rightarrow \frac{1}{4x^2y^2}$$